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Roll No:

### BTECH (SEM I) THEORY EXAMINATION 2021-22

**ENGINEERING MATHS-I** 

### Time: 3 Hours

Note: Attempt all Sections. If require any missing data; then choose suitably.

### **SECTION A**

### 1. Attempt all questions in brief.

a.	Find $y_n$ , if $y = x^2 e^{2x}$ .
b.	If $u(x,y) = (x^3 + x^3)^{\frac{1}{5}}$ , find the value of $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2}$ .
c.	If $z = u^2 + v^2$ , $u = r \cos \theta$ , $v = r \sin \theta$ find $\frac{\partial z}{\partial r}$ .
d.	Prove that $a^x = 1 + x \log a + \frac{x^2}{2!} (\log a)^2 + \frac{x^2}{3!} (\log a)^3 + \dots \dots \dots$
e.	Reduce the matrix $\begin{bmatrix} 1 & 1 & 1 \\ 2 & 3 & 1 \end{bmatrix}$ into normal form.
f.	Find the inverse of the matrix $A = \begin{bmatrix} 2 & 1 \\ 1 & 1 \end{bmatrix}$ .
g.	Evaluate $\Gamma\left(-\frac{3}{2}\right)$ .
h.	Evaluate $\int_0^{\pi} \int_0^{a \sin \theta} r dr d\theta$ .
i.	Show that $\vec{V} = (y+z)\hat{i} + (z+y)\hat{j} + (x+y)\hat{k}$ is solenoidal.
j.	Prove that $div(\emptyset \vec{a}) = \emptyset dv \vec{a} + (grad\emptyset) \cdot \vec{a}$
	SECTION B
2.	Attempt any <i>three</i> of the following: 10x3=30
a.	If $y = (sin^{-1}x)^2$ , show that $(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} - n^2y_n = 0$ and calculate $y_n(0)$ .
h	A rectangular box, open at the top, is to have given capacity. Find the dimensions of the box

b. requiring least material for its construction.

c.	Reduce the matrix $A = \begin{bmatrix} -1 & 2 & -2 \\ 1 & 2 & 1 \\ -1 & -1 & 0 \end{bmatrix}$ to the diagonal form.	
d.	Show that $\iiint \frac{dxdydz}{(x+y+z)^3} = \frac{1}{2}\log 2 - \frac{5}{16}$ . The integral being taken throughout the v bounded by $x = 0, y = 0, z = 0, x + y + z = 0$ .	olume
e.	Verify Stoke's theorem for $\vec{F} = x^2\hat{\imath} + xy\hat{\jmath}$ integrated round the square whose sides are $x = 0, y = 0, x = a, y$ in the plane $z = 0$ .	



Total Marks: 100

 $2 \ge 10 = 20$ 

Subject Code: NAS103



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10x1 = 10

10x1 = 10

10x1=10

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### **SECTION C**

### 3. Attempt any *one* part of the following:

a.	Trace the curve: $x^3 + y^3 - 3axy = 0$ .
b.	If $u = \frac{x^3y^3z^3}{x^3+y^3+z^3} + \log\left(\frac{xy+yz+zx}{x^2+y^2+z^2}\right)$ , then prove that $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} + z\frac{\partial u}{\partial z} = 6\frac{x^3y^3z^3}{x^3+y^3+z^3}$ .

### 4. Attempt any *one* part of the following:

# a. Expand x<sup>2</sup>y + 3y - 2 in powers of (x - 1) and (y + 2) using Taylor's Theorem. b. If u, v and w are the roots of (λ - x)<sup>3</sup> + (λ - y)<sup>3</sup> + (λ - z)<sup>3</sup> = 0, cubic in λ, find <sup>∂(u,v,w)</sup>/<sub>∂(x,y,z)</sub>.

### 5. Attempt any *one* part of the following:

a.	Investigate the values of $\lambda$ and $\mu$ so that the equations $2x + 3y + 5z = 9,7x + 3y - 2z = 8,2x + 3y + \lambda zhave \mu$ (a) no solution, (b) a unique solution and (c) an infinite number of solutions.
b.	Verify Cayley-Hamilton theorem for the matrix $A = \begin{bmatrix} 1 & 2 & 0 \\ 2 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$ and hence find $A^{-2}$ .

## 6. Attempt any one part of the following:

a.	Find the arc length of the curve $y = \sqrt{x}$ from $x = 0$ to $x = 4$ .
b.	Change the order of integration in $I = \int_0^1 \int_{x^2}^{2-x} xy dy dx$ and hence evaluate the same.

### 7. Attempt any *one* part of the following:

### 10x1=10

10x1 = 10

a.	Find the directional derivative $\emptyset d = (x^2 + y^2 + z^2)^{-\frac{1}{2}}$ at the point(3,1,2) in the direction of the vector $yz\hat{i} + zx\hat{j} + xy\hat{k}$ .
b.	Verify Green's theorem in the plane for $\oint_C [(x^2 - 2xy)dx + (x^2y + 3)dy]$ where <i>C</i> is the boundary of the region defined by $y^2 = 8x$ and $x = 2$ .

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